

15) Work out the multiplication table of the symmetry group of the proper covering operations of an equilateral triangle. Write down all the subgroups and divide the group elements into classes. What are the allowed dimensionalities of the representation matrices of the group?

PART – C

Answer any FOUR questions

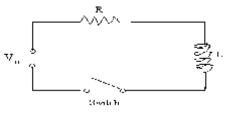
16) (a) Using the contour integration, show that $\int_{0}^{\infty} \frac{dx}{1+x^4} = \frac{\pi}{2\sqrt{2}}$.

(b) Evaluate the following integral using Cauchy's integral formula $\int_{c} \frac{4-3z}{z(z-1)(z-2)} dz$, where C is the

 $(4 \times 12.5 = 50)$

circle |Z| = 3/2.

17) Find the current i(t) in the LC circuit shown in figure by setting up the differential equation for the problem and solving it by Laplace transforms. Assume zero initial current and charge on the



capacitor and V_o, a constant voltage.

- 18) Solve the one- dimensional wave equation $\frac{\partial^2 u}{\partial t^2} = c^2 \frac{\partial^2 u}{\partial x^2}$ by the separation of variable technique and the use of Fourier series. The boundary conditions are u(0,t) = 0 and u(L,t) = 0 for all t and the initial conditions are u(x,0) = f(x) and $\frac{\partial u}{\partial t} = g(x)$ at t = 0. (Assume that u(x,t) to represent the deflection of stretched string and the string is fixed at the ends x = 0 and x = L).
- 19) (a) Solve the Legendre differential equation $(1 x^2) \frac{d^2y}{dx^2} 2x \frac{dy}{dx} + n (n+1)y = 0$ by the power series method.
 - (b) Establish the orthonormality relation $\int_{-1}^{+1} P_n(x) P_m(x) dx = \frac{2}{(2n+1)} \delta_{nm}$ where $P_n(x)$ is the

Legendre polynomial of order n.

20) (a) Prove that any representation by matrices with non-vanishing determinants is equivalent to a representation by unitary matrices.

(b)Enumerate and explain the symmetry elements of CO₂, H₂O and NH₃ molecules. ($6\frac{1}{2}+6$)
